

$$v = f / f_{\text{sample}}$$

$$W = 2 * \pi * v$$

$$\phi = W - \pi/2$$

$$z = \exp(j*W)$$

We need  $G(z) = -j$

Try

$$G(z) = \frac{\sin(\phi)}{\cos(\phi)} + \frac{1}{\cos(\phi)} * \exp(-j*W)$$

$$= \frac{\sin(W-\pi/2)}{\cos(W-\pi/2)} + \frac{1}{\cos(W-\pi/2)} * [\cos(W) + j \sin(W)]$$

$$1.) \quad \frac{\sin(W) * \cos(\pi/2) - \cos(W) * \sin(\pi/2)}{\cos(W) * \cos(\pi/2) - \sin(W) * \sin(\pi/2)} + \frac{1}{\cos(W) * \cos(\pi/2) - \sin(W) * \sin(\pi/2)} * [\cos(W) + j \sin(W)]$$

$$2.) \quad \frac{0 - \cos(W)}{0 - \sin(W)} + \frac{1}{0 - \sin(W)} * [\cos(W) + j \sin(W)]$$

$$= \frac{-\cos(W)}{-\sin(W)} + \frac{\cos(W)}{-\sin(W)} + \frac{j \sin(W)}{-\sin(W)}$$

$$= 0 + (-j)$$

$$= -j$$

1.) addition theorem

$$\sin(x-y) = \sin(x) * \cos(y) - \cos(x) * \sin(y)$$

$$\cos(x-y) = \cos(x) * \cos(y) - \sin(x) * \sin(y)$$

$$2.) \cos(\pi/2) = 0$$

$$\sin(\pi/2) = 1$$

so we make a fir filter:

$$y(k) = a_0 * x(k) + a_1 * x(k-1)$$

$$a_0 = \frac{\sin(\phi)}{\cos(\phi)} = \tan(\phi)$$

$$a_1 = 1/\cos(\phi)$$