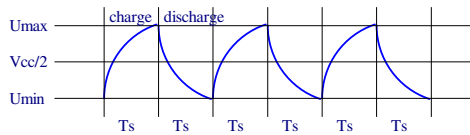


Ut charge/discharge



$U_{max} - U_{min} = V_{cc}/(2^N)$ N is resolution Ts is interrupt cycle time

charge ($U_x = V_{cc}$)

$$U_t(0) = U_{min}$$

$$U_t(T_s) = U_{min} \cdot e^{-K} + (U_{in}/2 + V_{cc}/2) \cdot (1 - e^{-K}) = U_{max} \quad (I)$$

discharge ($U_x = 0$)

$$U_t(0) = U_{max}$$

$$U_t(T_s) = U_{max} \cdot e^{-K} + (U_{in}/2) \cdot (1 - e^{-K}) = U_{min} \quad (II)$$

$$K = T_s / (C \cdot R/2) = (2^N) \cdot T_i / (C \cdot R/2)$$

Calculating I - II

$$(U_{min} - U_{max}) \cdot e^{-K} + (V_{cc}/2) \cdot (1 - e^{-K}) = U_{max} - U_{min}$$

Naming $U_{max} - U_{min}$ to U_{ripple}

$$(V_{cc}/2) \cdot (1 - e^{-K}) = U_{ripple} \cdot (1 + e^{-K})$$

$$e^{-K} = (V_{cc}/2 - U_{ripple}) / (V_{cc}/2 + U_{ripple})$$

substituting K and solving for RC

$$R \cdot C = 2 \cdot T_s / \ln((V_{cc}/2 + U_{ripple}) / (V_{cc}/2 - U_{ripple}))$$

Optimum value for $R \cdot C$

We want U_{ripple} to be less than $V_{cc}/(2^N)$

Substituting $U_{ripple} = V_{cc}/(2^N)$

$$R \cdot C = 2 \cdot T_s / \ln((2^N + 2) / (2^N - 2))$$

$$N = 1 / \ln((2^N + 2) / (2^N - 2))$$

$$8 = 64$$

$$9 = 128$$

$$10 = 256$$

$$11 = 512$$

$$12 = 1024$$

$$13 = 2048$$

$$14 = 4096$$

$$15 = 8192$$

From the table follows

$$1 / \ln((2^N + 2) / (2^N - 2)) = 2^{(N-2)}$$

$$R \cdot C = T_s \cdot 2^{(N-1)}$$